



Turbulent particle pinch in flux-driven ITG/TEM turbulence

Contents

1. GGHB project (1/24)
2. Development of global GK code with field aligned coordinates (11/24)
3. Turbulent particle pinch in flux-driven ITG/TEM turbulence (12/24)

Kenji IMADERA and Shuhei OKUDA

Graduate School of Energy Science, Kyoto University, Japan

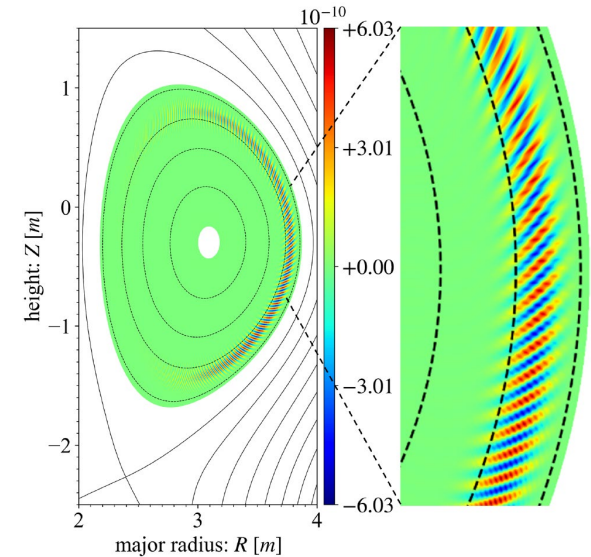
Project Members

Akihiro Ishizawa, Mikiya Muto, Shuhei Genko, Rintaro Matsumura (Kyoto U.)
Masatoshi Yagi, Haruki Seto (QST)

Digest of GGHB Project (2022)

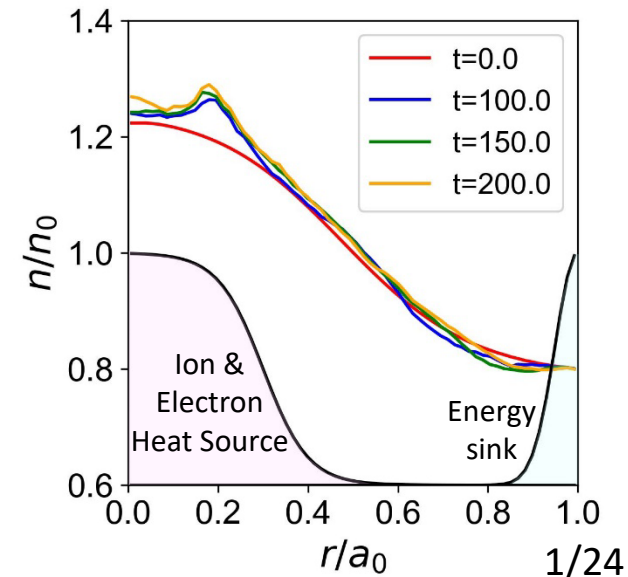
(A) Development of global GK code with field aligned coordinates [Okuda+, accepted to PFR]

- ✓ We have introduced the Field-Aligned Coordinates (FAC) with a shifted metric to our global gyrokinetic code GKNET and drastically reduced the computational cost.
- ✓ We have also implemented numerical magnetic equilibria and performed linear/nonlinear global δf simulation for the JT-60SA ITER-like plasma (Upper right).



(B) Turbulent particle pinch in flux-driven ITG/TEM turbulence [Imadera+, submitted to FAC-2023]

- ✓ By means of GKNET with the hybrid electron model, we have investigated flux-driven ITG/TEM turbulence.
- ✓ We have found that turbulence directly/indirectly drives ion particle pinch under ion/electron heating, leading to the synergetic density peaking of bulk ions (Bottom right).



Development of global GK code with FAC

For tokamak core/edge turbulence global simulations, we have developed GKNET-FAC, which includes the following two advances :

A : Field-aligned coordinate system (FAC)

- Significantly reduce the computational cost.
- A shifted metric technique [B.Scott, PoP-2001] is used to correct a cell deformation. (not included in this report)

B : Connection with a 2D equilibrium code

- Allow for simulations with realistic tokamak equilibria.



C : We have applied to a nonlinear simulation of ITG instability in a **JT-60SA plasma** [S.Okuda, PFR-2023].

A : Field-aligned coordinates - 1

Field-aligned coordinates

[Beer+, PoP-1995]

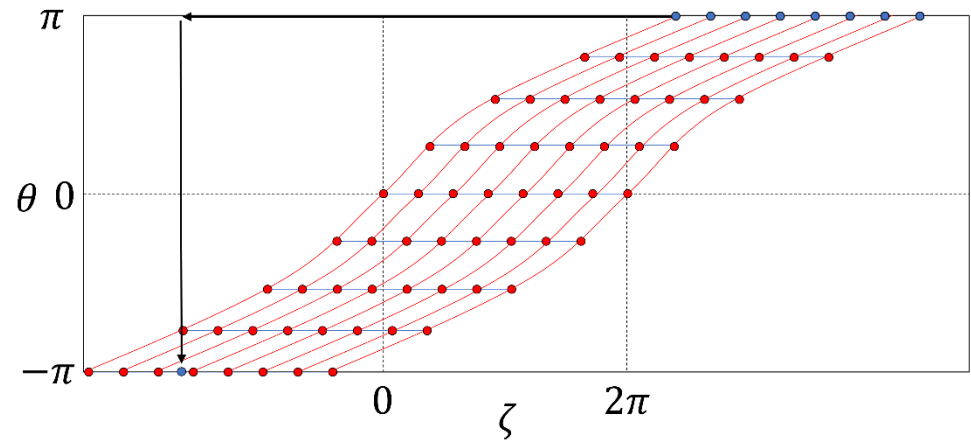
$$\begin{aligned}x &= \rho & [0, 1] \\y &= y_{\text{shift}} - \zeta & [0, 2\pi) \\z &= \theta - \theta_0 & [-\pi, \pi)\end{aligned}$$

$$y_{\text{shift}} = \int_{\theta_0}^{\theta} v(\rho, \theta') d\theta'$$

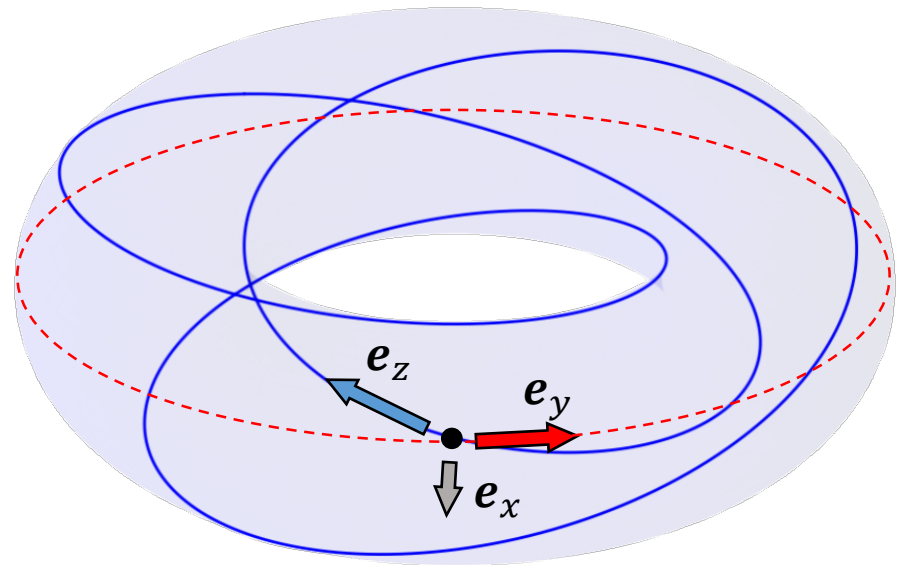
$$v = \frac{\mathbf{B} \cdot \nabla \zeta}{\mathbf{B} \cdot \nabla \theta}$$

- The direction of \mathbf{e}_z is along the field line.

$$\mathbf{e}_z = \mathbf{e}_\theta + v\mathbf{e}_\zeta = \mathbf{B}/B_\theta$$



Computational grids on a flux surface



Covariant basis vectors
with a field line(blue)

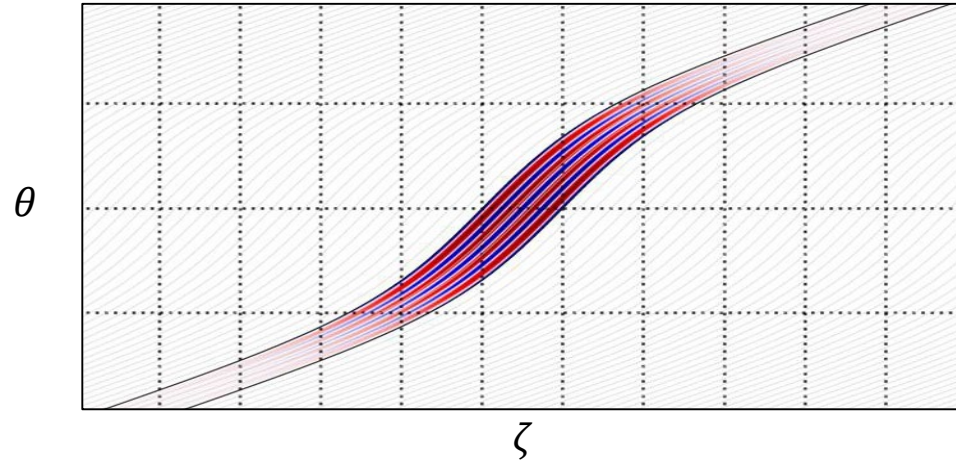
A : Field-aligned coordinates - 2

- Wavenumbers of resonant instabilities are low in the direction along the magnetic field line.

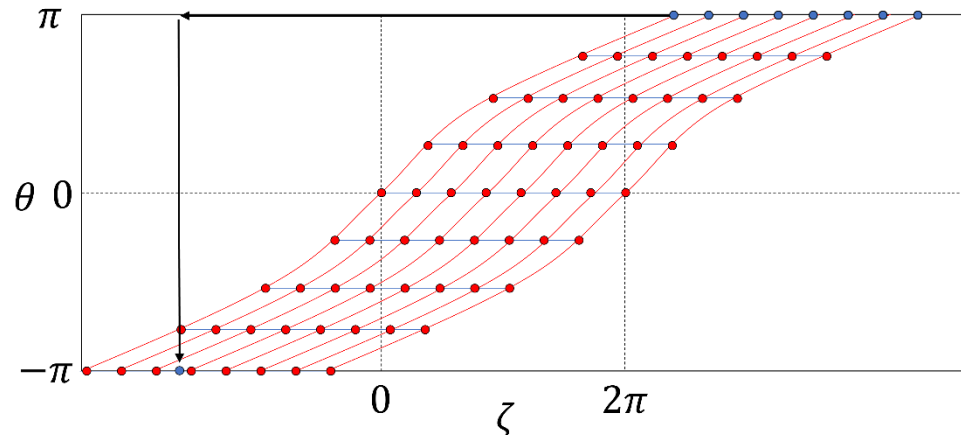


- By using a coordinate along the field lines, instabilities can be resolved **with a small number of computational grids**.
- It is particularly **effective in the edge regions** where the higher poloidal mode numbers resonate with the higher q values.

Ideal ballooning mode (n=20)

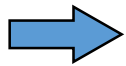


Computational grids of FAC



A : Field-aligned coordinates - 3

Simulations of the linear ITG instability were performed on GKNET-FAC and conventional GKNET.



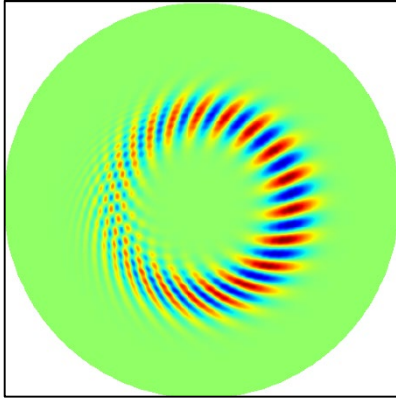
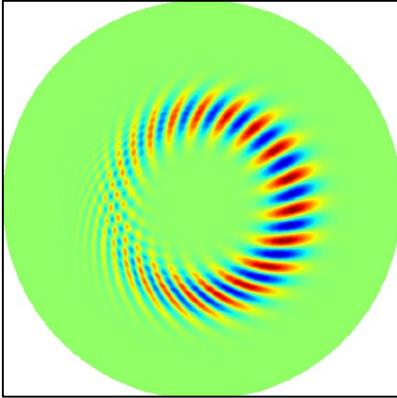
Are the results consistent?
How much computation time was reduced?

Simulation condition : concentric circular torus with the CBC parameters :

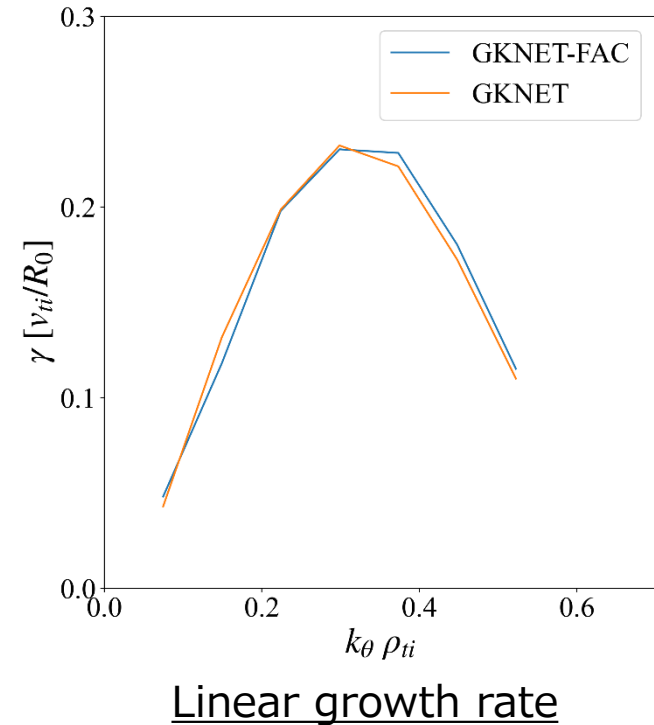
$$\frac{a_0}{R_0} = 0.36, \quad \frac{R_0}{L_n} = 2.22, \quad \frac{R_0}{L_{Ti}} = \frac{R_0}{L_{Te}} = 6.92, \quad q = 0.85 + 2.18 \left(\frac{r}{a_0} \right)^2$$

- δf global model with the adiabatic electron.
- The radial domain is set to $0.1 < \rho < 1$.
- 1/4 wedge torus is assumed.
- 128CPU on JFRS-1 are used.
- $a_0/\rho_{ti} = 150$

A : Field-aligned coordinates - 4

	Conventional GKNET	GKNET-FAC
$\phi_{n=16}$		
Required grids	$(N_\rho, N_\zeta, N_\theta, N_{v_\parallel}, N_\mu)$ = (128, 48, 256, 80, 16)	$(N_x, N_y, N_z, N_{v_\parallel}, N_\mu)$ = (128, 48, 16, 80, 16)
Time per 1 step	4.02 [s]	0.55 [s]

1/16 (between Required grids) and 1/7.3 (between Time per 1 step)



- Both results are consistent.
- The number of time steps required is reduced to **1/5**.
- The computation time is reduced to $1/7.3 \times 1/5 = 1/36.5$ (**=2.7%**).

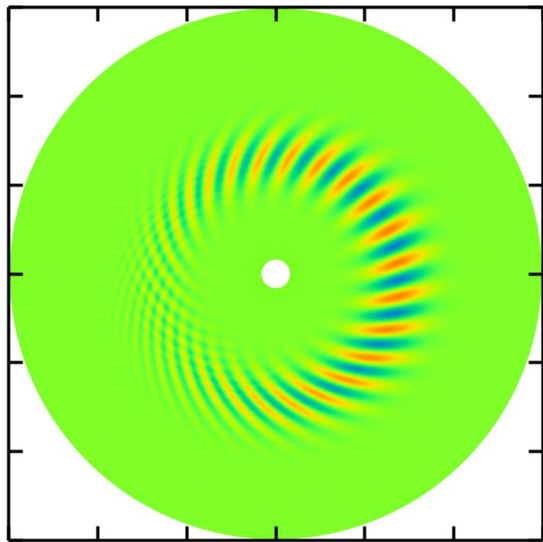
B : Realistic tokamak equilibria

Conventional GKNET

Equilibrium is set by functions.

$$\mathbf{B} = \frac{R_0}{qR^2} \mathbf{e}_\theta + \frac{R_0}{R^2} \mathbf{e}_\zeta$$

B^θ B^ζ

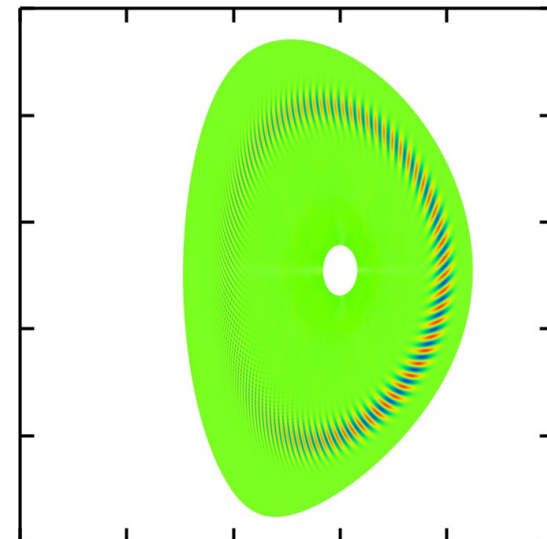


GKNET-FAC

Equilibrium is set by numerical data of a realistic tokamak equilibrium.

```
+7.996469528537010E-001 +1.002618860547062E+000  
+7.996468322475245E-001 +1.002618709327794E+000  
+7.996461323977480E-001 +1.002617831837318E+000  
+7.996448537145523E-001 +1.002616228589929E+000  
+7.996429968363297E-001 +1.002613900386063E+000  
+7.996405627062098E-001 +1.002610848408238E+000  
+7.996375525050876E-001 +1.002607074137095E+000
```

B^θ B^ζ



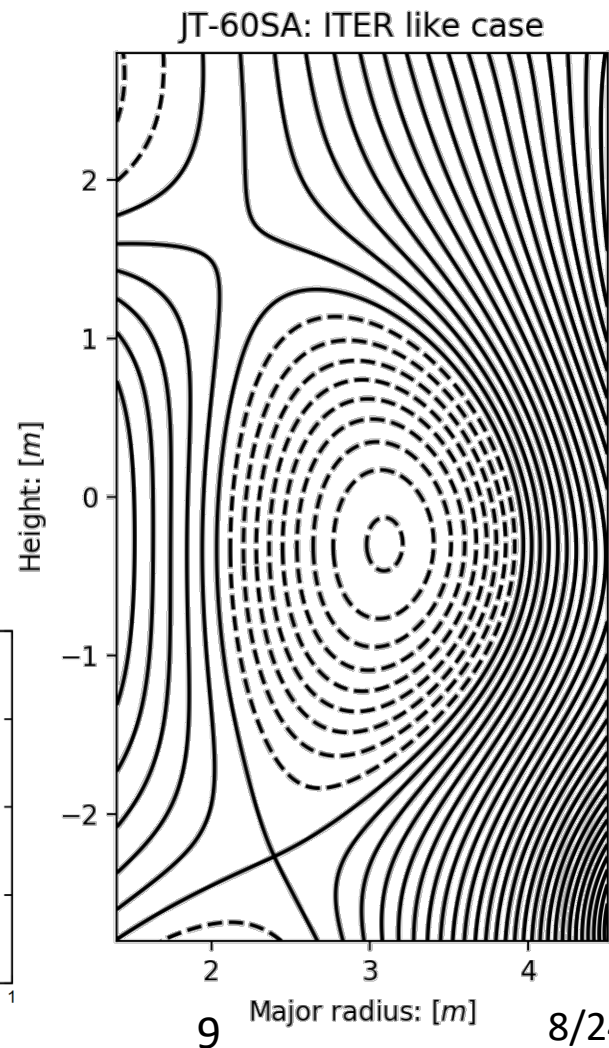
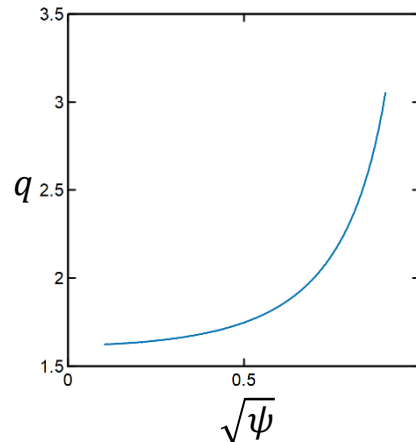
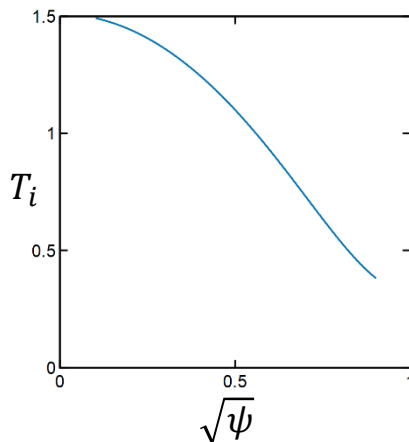
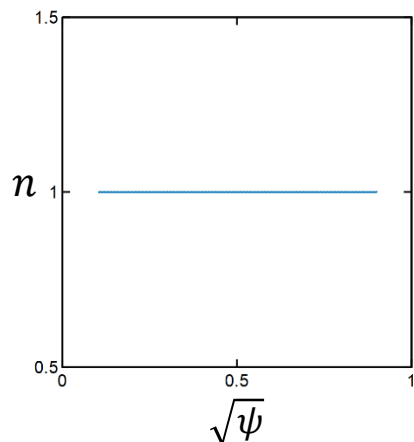
- GKNET-FAC can now handle arbitrarily shaped equilibria, including vertically asymmetric equilibria, which could not be handled by the conventional GKNET.

C : Nonlinear simulation of the JT-60SA plasma - 1

Finally, we have performed the nonlinear ITG simulation using the JT-60SA plasma [M.Nakata+, PFR-2014] on GKNET-FAC.

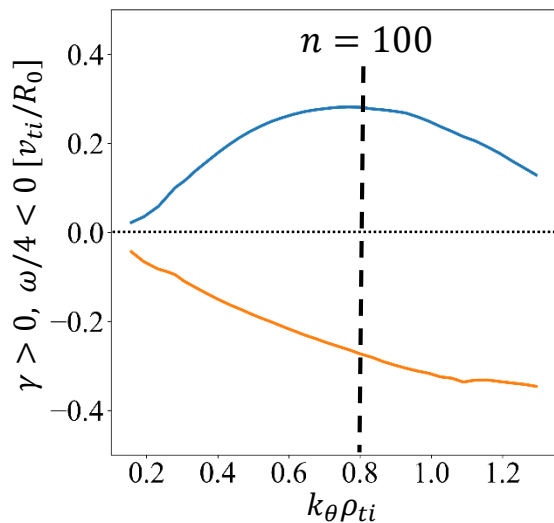
Simulation conditions :

- δf global model with the adiabatic electron.
- The radial domain is set to $0.1 < \sqrt{\psi} < 0.9$.
- 1/4 wedge torus is assumed.
- 10240CPU on JFRS-1 are used.
- $a_0/\rho_{ti} = 294$
- $(N_x, N_y, N_z, N_{v_{\parallel}}, N_{\mu}) = (720, 256, 32, 80, 16)$

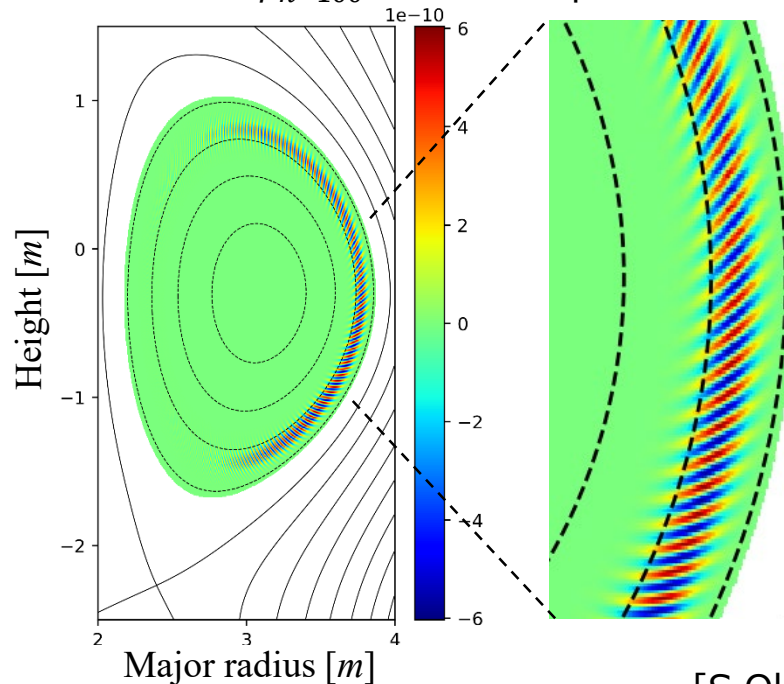


C : Nonlinear simulation of the JT-60SA plasma - 2

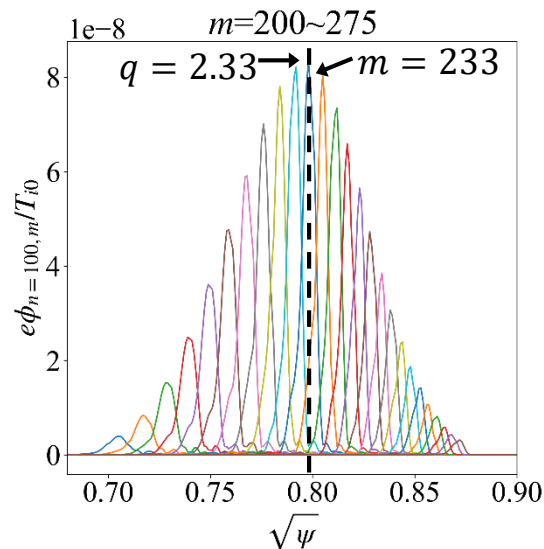
Dispersion relation



$\phi_{n=100}$ in a linear phase



The poloidal harmonics of $\phi_{n=100}$

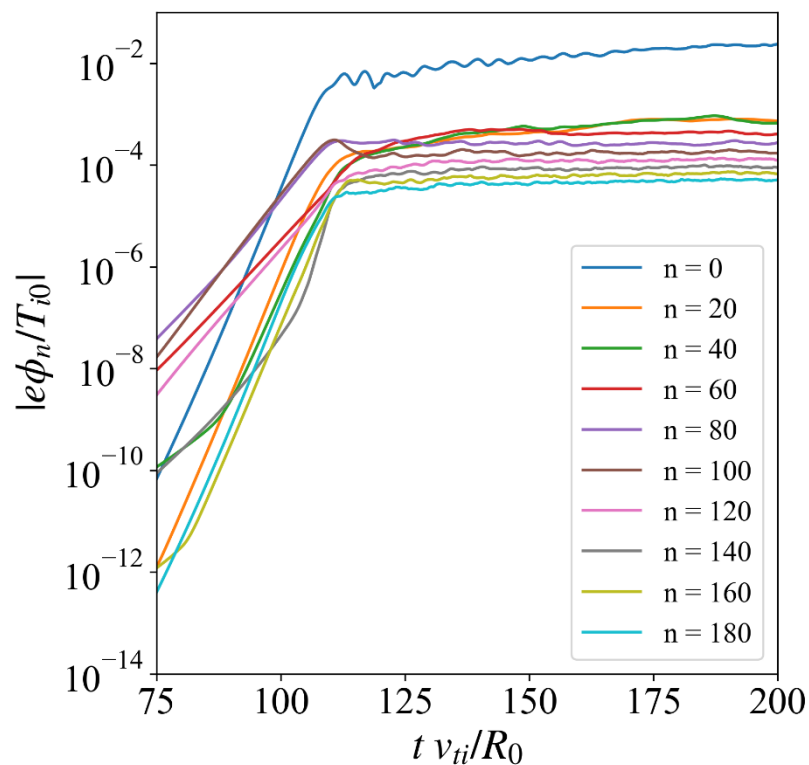


[S.Okuda, PFR-2023]

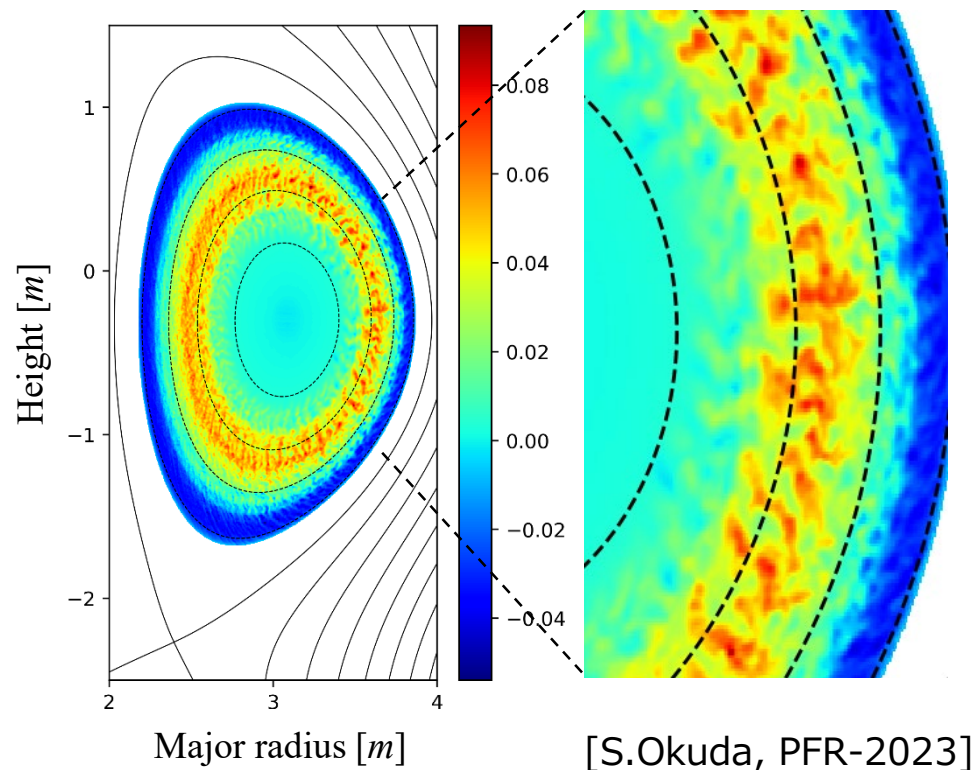
- Very high poloidal mode number instabilities, such as $(m, n) = (233, 100)$, have been resolved.

C : Nonlinear simulation of the JT-60SA plasma - 3

Time development of the amplitude of the electrostatic potential



$\phi(\zeta = 0)$ after the nonlinear saturation



- The zonal flow has been generated at the position corresponding to the linear instabilities.

C : Nonlinear simulation of the JT-60SA plasma - 4

- Consider the number of meshes required to resolve the mode $m_{\text{res}} = 160 \times 2.3 \approx 370$ resonating with $n = 160$, which is unstable in this case.
 - Assume that 8 times as many meshes as the mode number are required.
 - If (ρ, θ, ζ) coordinates is used, $N_{\theta} = 370 \times 8 \approx 3000$ is required.
 - If FAC is used, $N_z = 32$ is enough as this case.
 - Due to FAC, the required meshes are reduced to $32 \div 3000 \approx 1/94$.
- For a simulation up to $t v_{ti}/R_0 = 200$, it took **12.5 hours using 10240CPU on JFRS-1.**

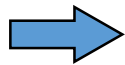


It cannot be calculated without using FAC.

Summary and future plans

- Summary

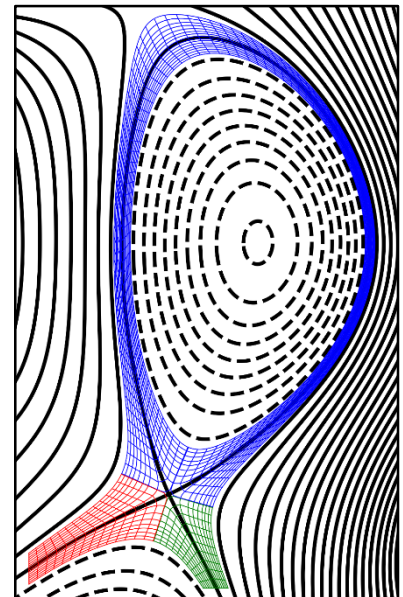
- The field-aligned coordinate system has been successfully implemented into GKNET.
- GKNET has been connected with a 2D equilibrium code.



It is now possible to simulate instabilities in large scale realistic tokamak equilibria such as JT-60SA.

- Future plans

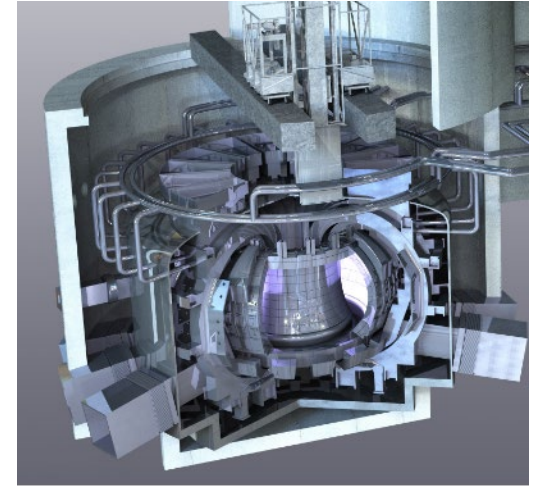
- The development of GKNET will be extended to address tokamak edge turbulence.
- Currently, an interface code is being developed to generate a computational grid in the SOL/divertor region.



Background: Refueling by Particle Pinch

- ✓ Establishment of a refueling method is an important issue to control nuclear fusion reactors.
- ✓ But, in DEMO-class high-temperature plasmas, a pellet injection reaches only up to 80-90% of the minor radius so that the central density peaking depends on particle pinch, making the prediction difficult.
- ✓ While turbulent particle transport has been studied based on local gyrokinetic models, it is important to study global physics.
- ✓ The above analysis is also meaningful to investigate impurity transport such as Helium ash exhaust.

Schematic picture of
Japan-DEMO*



*[<https://www.fusion.qst.go.jp/rokkasyo/ddjst/>]

Background: Related Theory & Simulation

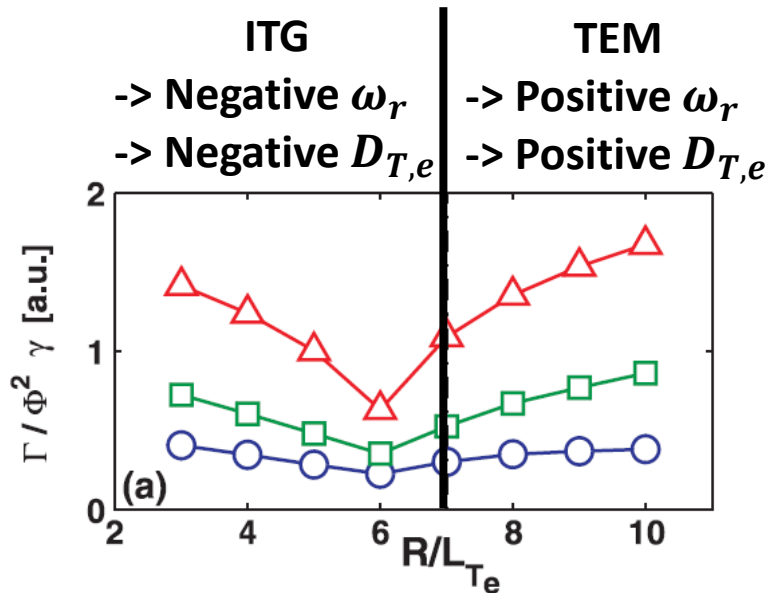
Turbulent particle flux calculated by fluid theory

[Nordman+, NF-1990]

$$\Gamma_s = \underbrace{D_{n,s} \frac{R}{L_{n,s}}}_{(1)} + \underbrace{D_{T,s} \frac{R}{L_{T,s}}}_{(2)} \quad D_{T,s} = -\frac{4L_{n,s}}{L_B} \left(\frac{10}{3} \frac{L_{n,s}}{L_B} - \frac{\omega_{r,s}}{\omega_{*,e}} \right)$$

Turbulent particle flux calculated by GS2 simulation

[Angioni+, NF-2004]

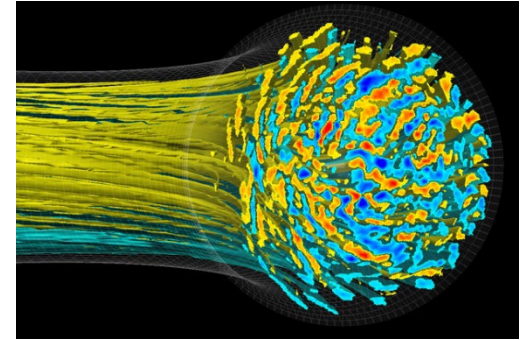


- ✓ Turbulent particle flux mainly is provided by (1) the diagonal diffusion term and (2) the non-diagonal thermo-diffusion term.
- ✓ While the sign of (1) is usually positive, that of (2) can become negative, depending on the real frequency, etc.
- ✓ In fact, the turbulent particle flux shows the opposite tendency for temperature gradient between ITG and TEM.

Purpose of This Research

- ✓ In order to understand such view points, we perform flux-driven ITG/TEM simulations in the presence of ion/electron heating by means of the full- f electrostatic version of our global gyrokinetic code GKNET with hybrid kinetic electron dynamics.

3D turbulence structure of ϕ
calculated by GKNET



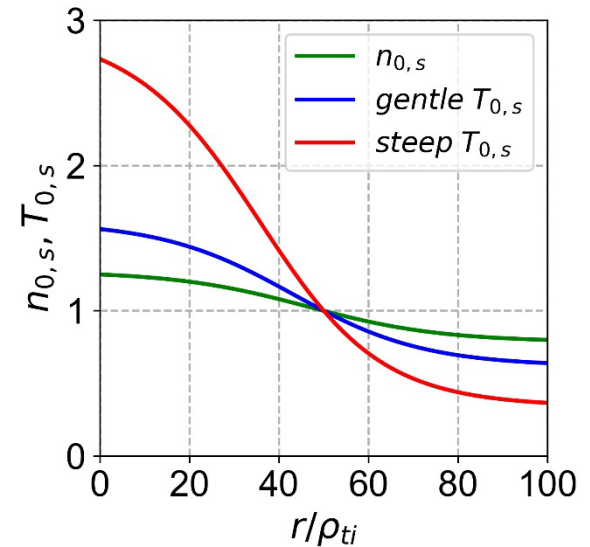
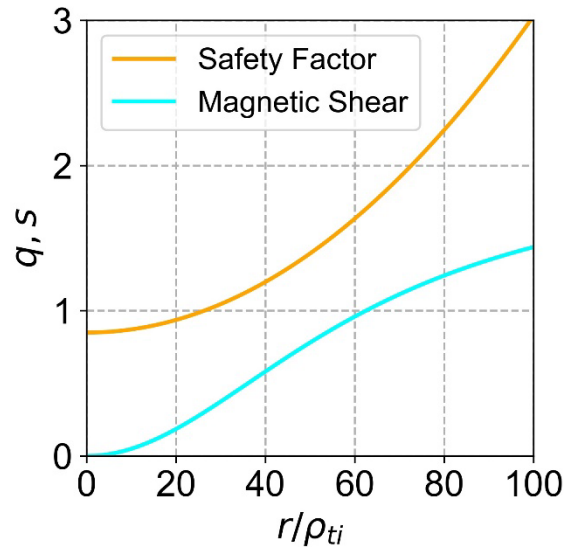
- ✓ First, we investigate the effect of ion/electron heating on the density peaking or flattening.
- ✓ Second, we separately discuss **turbulent particle transport by (1) the $E \times B$ drift with $n \neq 0$, (2) the $E \times B$ drift with $n = 0$, and (3) the magnetic drift ($n = 0$)** in addition to their physical mechanisms.

$$\frac{dE_r}{dt} = \Gamma_{i,E \times B(n \neq 0)} + \Gamma_{i,E \times B(n = 0)} + \Gamma_{i,B} - \Gamma_{e,E \times B(n \neq 0)} - \Gamma_{e,E \times B(n = 0)} - \Gamma_{e,B}$$

Simulation Condition

Simulation condition

Parameter	Value
a_0/ρ_i	100
a_0/R_0	0.36
$(R_0/L_n)_{r=a_0/2}$	2.22
Δ_r	30
$\sqrt{m_i/m_e}$	10
v_i^*	0.025
v_e^*	0.025



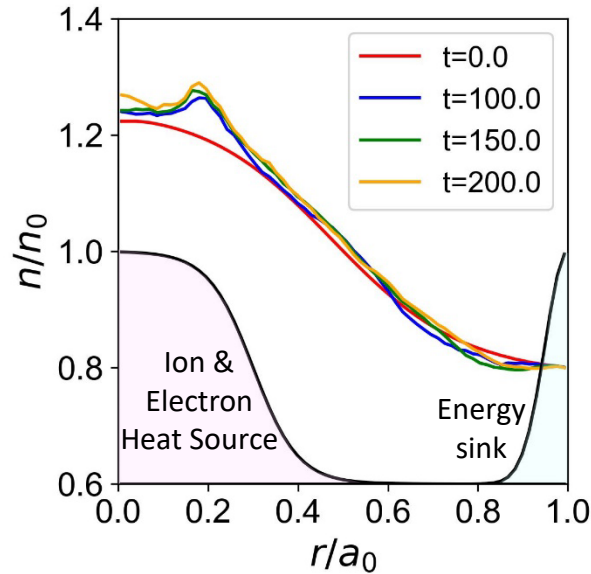
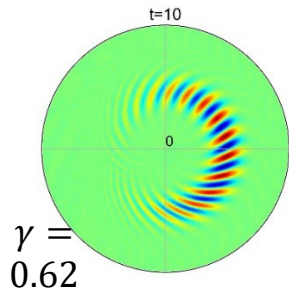
- ✓ In this study, we use GKNET-HE, the full- f electrostatic version with hybrid electron model.
- ✓ Here we consider three cases: (A) Mix ($R_0/L_{T_i} = 10$, $R_0/L_{T_e} = 10$) under ion/electron heating, (B) ITG ($R_0/L_{T_i} = 10$, $R_0/L_{T_e} = 4$) under ion heating, (C) TEM ($R_0/L_{T_i} = 4$, $R_0/L_{T_e} = 10$) under electron heating.

Density Peaking/Flattening

(A) Mix

$$R_0/L_{T_i} = 10$$

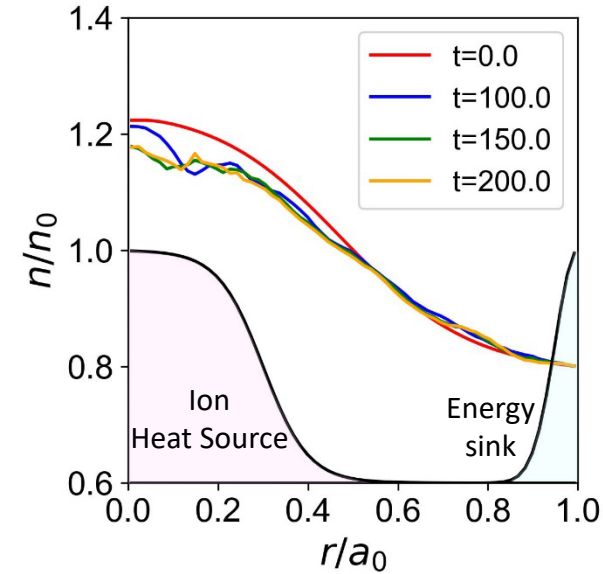
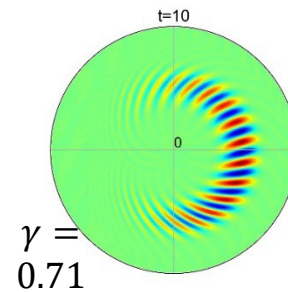
$$R_0/L_{T_e} = 10$$



(B) ITG

$$R_0/L_{T_i} = 10$$

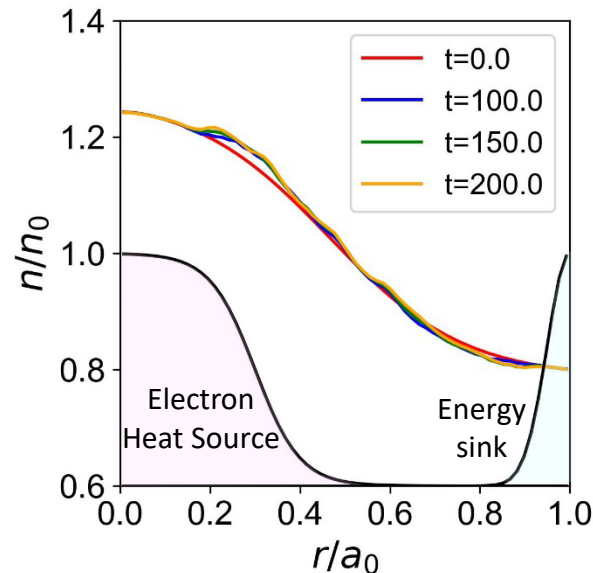
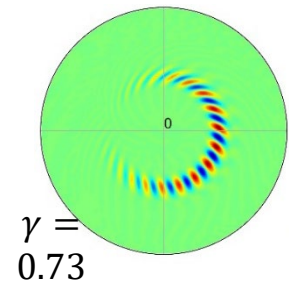
$$R_0/L_{T_e} = 4$$



(C) TEM

$$R_0/L_{T_i} = 4$$

$$R_0/L_{T_e} = 10$$



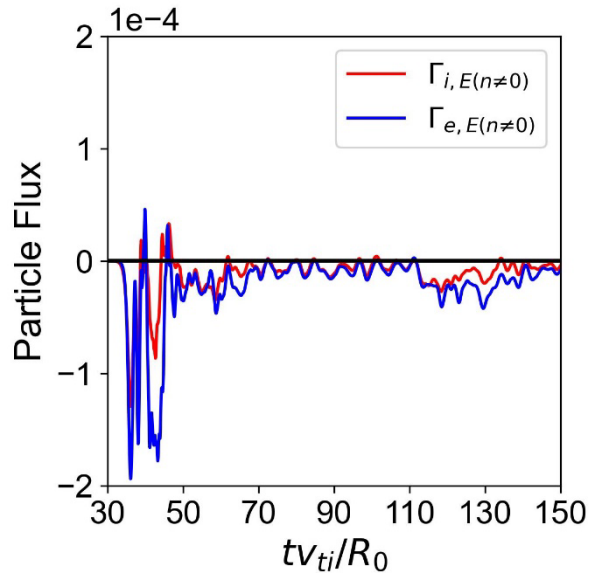
- ✓ While density profile are flattened by outer particle flux in the case (B), a density peaking can be observed in the case (A).
- ✓ The eigen structures (obtained by linear δf simulations) are almost same between the cases (A) and (B).

Particle Transport by $E \times B$ Drift ($n \neq 0$) - 1

(A) Mix

$$R_0/L_{T_i} = 10$$

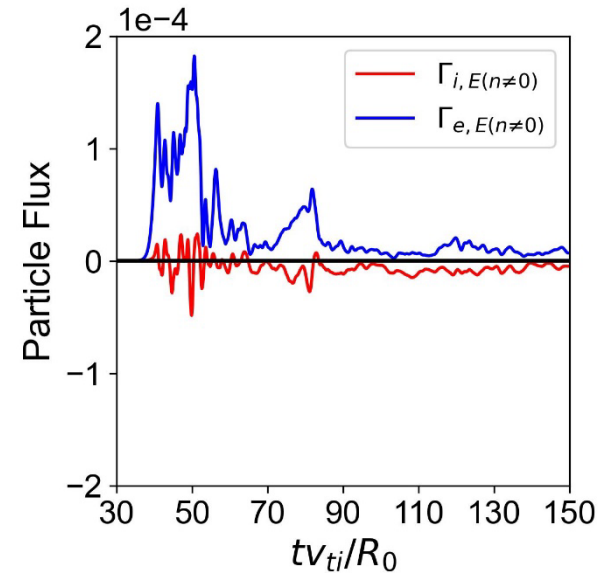
$$R_0/L_{T_e} = 10$$



(B) ITG

$$R_0/L_{T_i} = 10$$

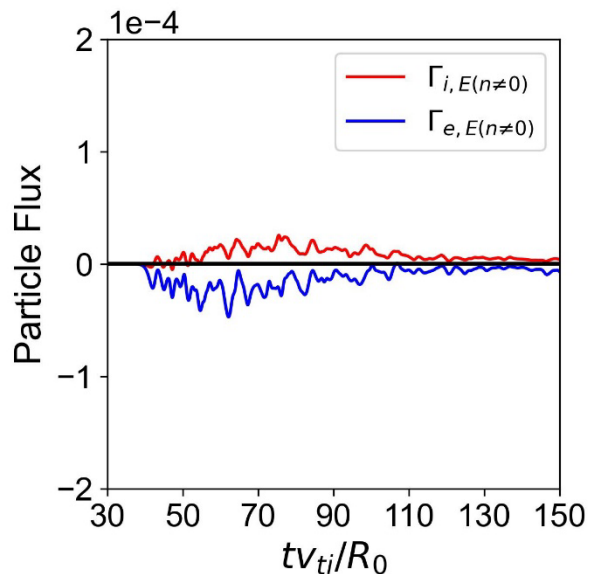
$$R_0/L_{T_e} = 4$$



(C) TEM

$$R_0/L_{T_i} = 4$$

$$R_0/L_{T_e} = 10$$



- ✓ When ion/electron temperature gradients are steep and sustained by ion/electron heating, inward particle transport (particle pinch) can be observed.

Particle Transport by $E \times B$ Drift ($n \neq 0$) - 2

Turbulent particle flux by fluid theory

[Nordman+, NF-1990]

$$\Gamma_s = \underbrace{D_{n,s} \frac{R}{L_{n,s}}}_{\text{Positive}} + \underbrace{D_{T,s} \frac{R}{L_{T,s}}}_{\text{Negative}} \quad D_{T,s} = -\frac{4L_{n,s}}{L_B} \left(\frac{10}{3} \frac{L_{n,s}}{L_B} - \frac{\omega_{r,s}}{\omega_{*,e}} \right)$$

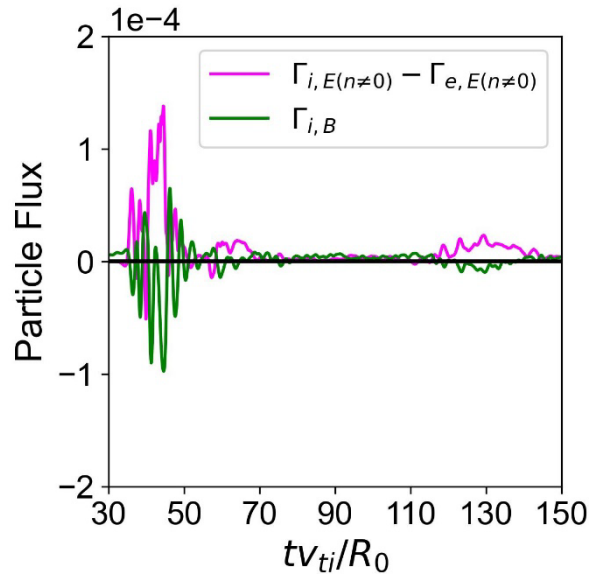
- ✓ In the present cases, $L_{n,s}/L_B \sim 1/2.22$ and $0.5 < \omega_{r,TEM}/\omega_{*,e} < 1$ are assumed so that $D_{T,s}$ is still negative even in the TEM case.
- ✓ When the temperature gradient is steep, the non-diagonal thermo-diffusion term becomes dominant, leading to the inward particle transport.
- ✓ As the result, the balance of particle fluxes breaks, leading to the charge separation.

	$\frac{R_0}{L_{T_i}} = 10, \frac{R_0}{L_{T_e}} = 10$	$\frac{R_0}{L_{T_i}} = 10, \frac{R_0}{L_{T_e}} = 4$	$\frac{R_0}{L_{T_i}} = 4, \frac{R_0}{L_{T_e}} = 10$
$\Gamma_{i,E(n \neq 0)}$	Negative	Weakly Negative	Weakly Positive
$\Gamma_{e,E(n \neq 0)}$	Strongly Negative	Positive	Weakly Negative
$\Gamma_{i,E(n \neq 0)} - \Gamma_{e,E(n \neq 0)}$	Positive	Negative	Positive

Ion Particle Transport by Magnetic Drift (n=0) - 1

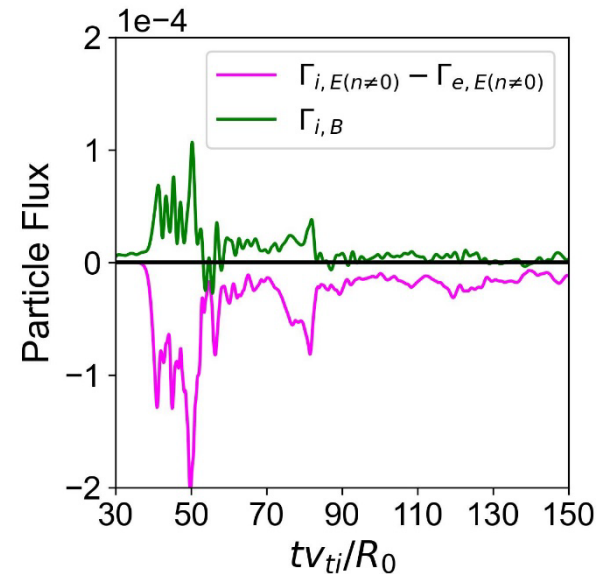
(A) Mix

$$R_0/L_{T_i} = 10$$
$$R_0/L_{T_e} = 10$$



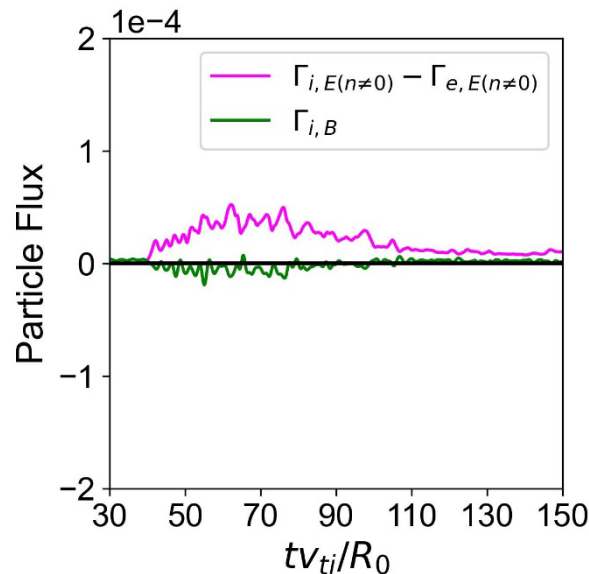
(B) ITG

$$R_0/L_{T_i} = 10$$
$$R_0/L_{T_e} = 4$$



(C) TEM

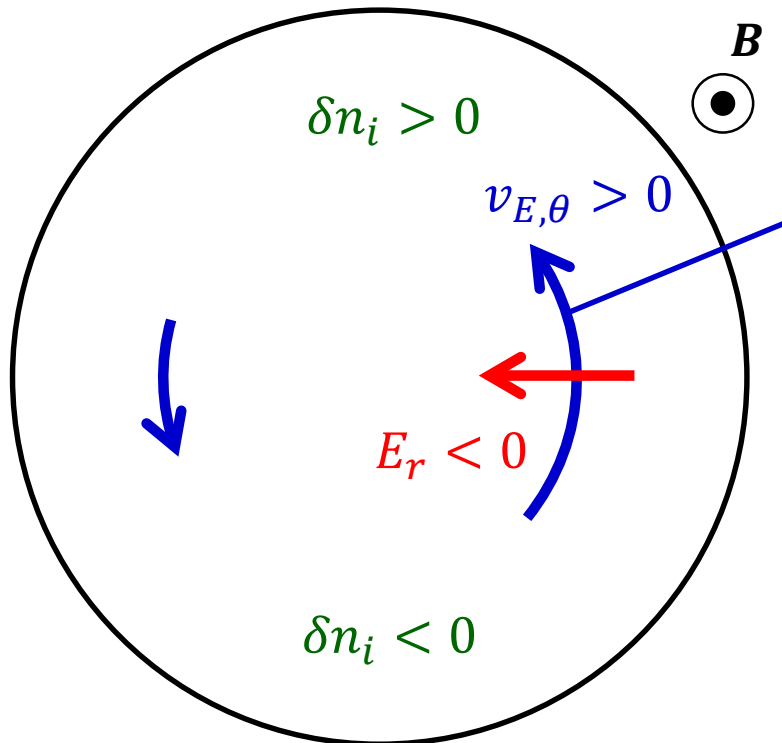
$$R_0/L_{T_i} = 4$$
$$R_0/L_{T_e} = 10$$



- ✓ When the $E \times B$ drift ($n \neq 0$) drives particle transport, the particle transport by the magnetic drift ($n=0$) is enhanced, which cancels with the $E \times B$ drift ($n \neq 0$) driven transport.
- ✓ Such a tendency was observed in the impurity transport [Idomura+, PoP-2021].

Ion Particle Transport by Magnetic Drift ($n=0$) - 2

- ✓ When $\Gamma_{i,E(n \neq 0)} - \Gamma_{e,E(n \neq 0)} > 0$, **negative mean radial electric field E_r** with $(m, n) = (0, 0)$ is triggered as below.
- ✓ Resultant **poloidal $E \times B$ flow $v_{E,\theta}$** has a poloidal up-down asymmetry, leading to **ion density perturbations with $(m, n) = (1, 0)$** .
- ✓ Such density perturbations can provide negative particle flux by magnetic drift.



$$v_{E,\theta} = -\frac{1}{B} E_r = -\left(1 + \frac{r}{R_0} \cos \theta\right) E_r$$



$$\frac{\partial \delta n_i}{\partial t} = -\frac{1}{r} \frac{\partial v_{E,\theta}}{\partial \theta} n_0 = -\frac{1}{R_0} E_r n_0 \sin \theta$$



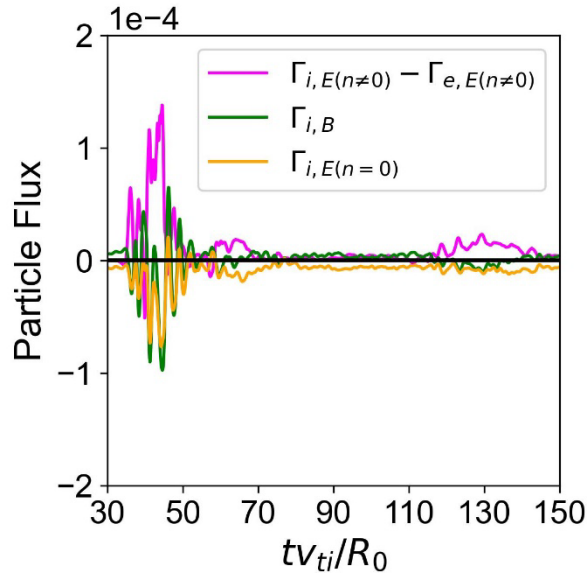
$$\frac{\partial}{\partial t} \langle v_{B,r} \delta n_i \rangle_f \propto E_r \langle \sin^2 \theta \rangle_f < 0$$

Ion Particle Transport by $E \times B$ Drift ($n=0$)

(A) Mix

$$R_0/L_{T_i} = 10$$

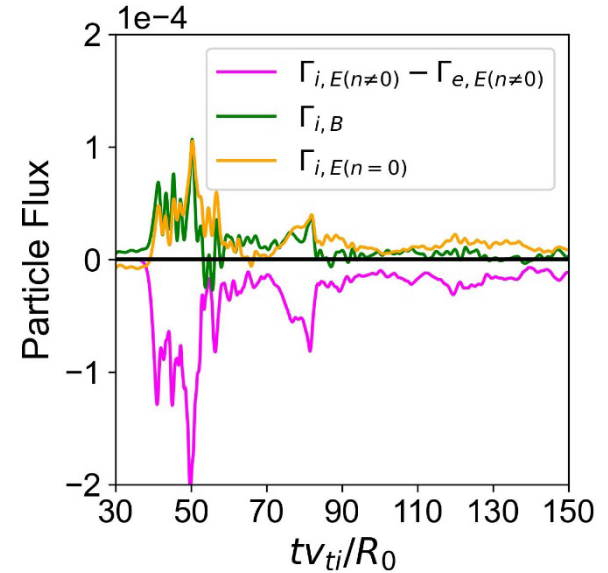
$$R_0/L_{T_e} = 10$$



(B) ITG

$$R_0/L_{T_i} = 10$$

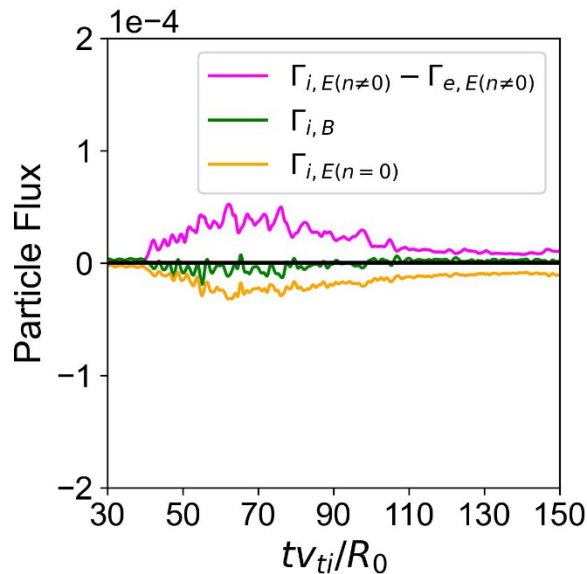
$$R_0/L_{T_e} = 4$$



(C) TEM

$$R_0/L_{T_i} = 4$$

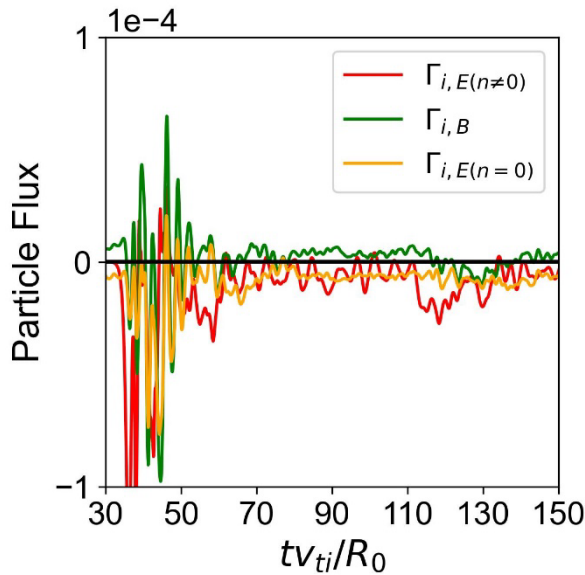
$$R_0/L_{T_e} = 10$$



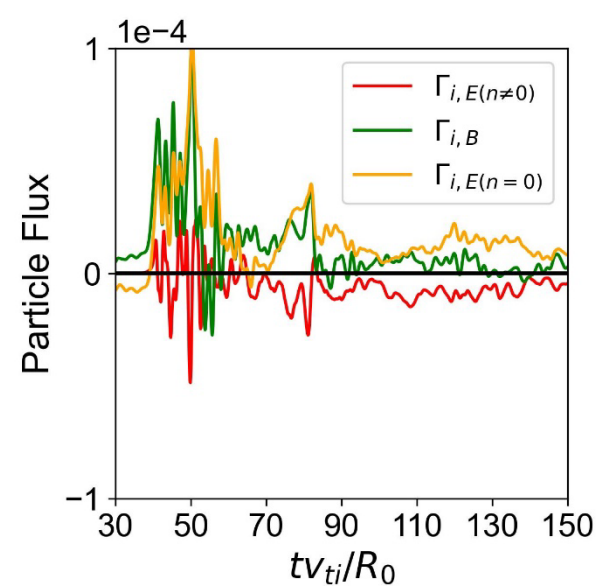
- ✓ It is newly found that particle transport by not only magnetic drift ($n=0$) but also $E \times B$ drift ($n=0$) are enhanced, which also cancels with $E \times B$ drift ($n \neq 0$) driven transport.

Summary of Turbulent Ion Particle Pinch

(A) Mix
 $R_0/L_{T_i} = 10$
 $R_0/L_{T_e} = 10$



(B) ITG
 $R_0/L_{T_i} = 10$
 $R_0/L_{T_e} = 4$



Step-1: Particle transport by $E \times B$ drift ($n \neq 0$) determined by temperature gradients

$$\underbrace{\Gamma_{i,E(n \neq 0)}}_{\text{Negative}} + \Gamma_{i,E(n=0)} + \Gamma_{i,B} - \underbrace{\Gamma_{e,E(n \neq 0)}}_{\text{Strongly Positive}} = 0$$

$$\underbrace{\Gamma_{i,E(n \neq 0)}}_{\text{Weakly Negative}} + \Gamma_{i,E(n=0)} + \Gamma_{i,B} - \underbrace{\Gamma_{e,E(n \neq 0)}}_{\text{Negative}} = 0$$

Step-2: Particle transport by $E \times B$ ($n=0$) and magnetic drift to satisfy the above balance

$$\underbrace{\Gamma_{i,E(n \neq 0)}}_{\text{Negative}} + \underbrace{\Gamma_{i,E(n=0)}}_{\text{Negative}} + \underbrace{\Gamma_{i,B}}_{\text{Weakly Negative}} - \underbrace{\Gamma_{e,E(n \neq 0)}}_{\text{Strongly Positive}} = 0$$

$$\underbrace{\Gamma_{i,E(n \neq 0)}}_{\text{Weakly Negative}} + \underbrace{\Gamma_{i,E(n=0)}}_{\text{Positive}} + \underbrace{\Gamma_{i,B}}_{\text{Positive}} - \underbrace{\Gamma_{e,E(n \neq 0)}}_{\text{Negative}} = 0$$

Summary

- ✓ We have performed flux-driven ITG/TEM simulations in the presence of ion/electron heating by means of the full- f electrostatic version of our global gyrokinetic code GKNET with kinetic electron dynamics.
- ✓ Enough steep ion temperature gradient can directly provide ion particle pinch by $E \times B$ drift ($n \neq 0$) through the thermo-diffusion term.
- ✓ Enough steep electron temperature gradient can also provide electron particle pinch, which can indirectly trigger ion particle pinch by $E \times B$ ($n=0$) and magnetic drifts through the ambipolarity condition.
- ✓ These two findings indicate that turbulence directly/indirectly drives ion particle pinch under ion/electron heating, leading to the synergetic density peaking of bulk ions.

$$\underbrace{\Gamma_{i,E \times B}(n \neq 0)}_{\substack{\text{Become negative} \\ \text{by steep } T_i \text{ gradient}}} + \underbrace{\Gamma_{i,E \times B}(n=0) + \Gamma_{i,B}}_{\substack{\text{Become negative} \\ \text{to satisfy} \\ \text{this condition}}} - \underbrace{\Gamma_{e,E \times B}(n \neq 0)}_{\substack{\text{Become positive} \\ \text{by steep } T_e \text{ gradient}}} = \cancel{\Gamma_{e,E \times B}(n=0)} - \cancel{\Gamma_{e,B}} = 0$$

Canceled with each other